

# Fluid dynamics and rheology in bifurcation lesions



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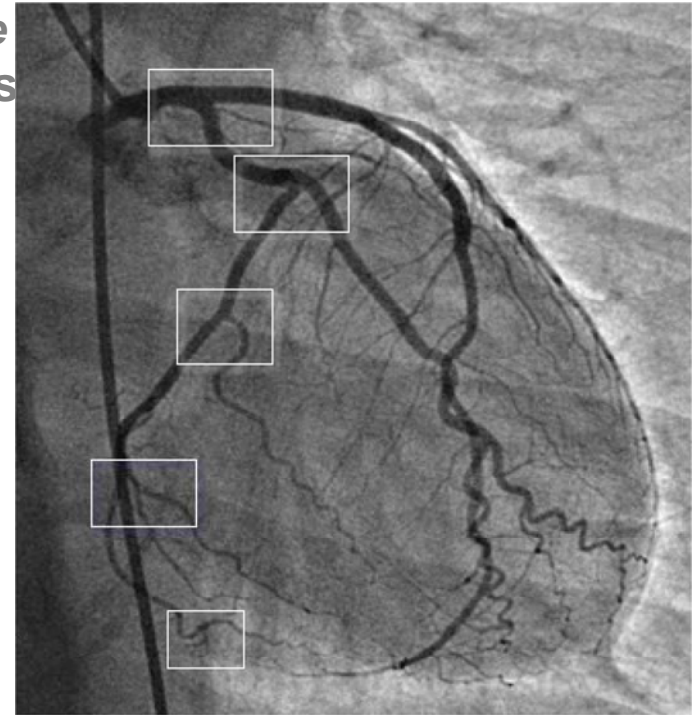
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**Inserm**  
Institut national  
de la sant  et de la recherche m dicale

*The geometry of Nature*  
Coronary artery bifurcations



*Finet G. et al. EuroIntervention 2007*

Vascular branching :

- ***distributive function***
- ***hemodynamic function***

## Multi-scale analysis

Quantification of coronary artery bifurcations according to mother-vessel diameter

Values obtained on quantitative coronary bifurcation angiography

	For all
# of bifurcation	173
$D_m$ (mean $\pm$ SD)	3.339 $\pm$ 0.948
$D_{d\text{-larger}}$ (mean $\pm$ SD)	2.708 $\pm$ 0.774
$D_{d\text{-smaller}}$ (mean $\pm$ SD)	2.236 $\pm$ 0.689
Reduction in mm (mean $\pm$ SD)	0.631 $\pm$ 0.365
% reduction	18.9
<b>Mean ratio</b>	<b>0.678</b>

*Variables are presented as mean  $\pm$  SD*  
*D in mm*  
 *$D_m$ : Diameter of the mother vessel*  
 *$D_{d\text{-larger}}$ : Diameter of the larger daughter vessel*  
 *$D_{d\text{-smaller}}$ : Diameter of the smaller daughter vessel*  
*Reduction: difference between the diameter of mother vessel and the diameter of the larger daughter vessel*  
*Ratio:  $D_m / (D_{d\text{-larger}} + D_{d\text{-smaller}})$*

$$R = \frac{D_{\text{mother}}}{D_{\text{daughter 1}} + D_{\text{daughter 2}}}$$

For an incompressible fluid,

The continuity formula is:  **$Q_{o1}+Q_{o2}=Q_i$**

$Q=SV$

If  $V=\text{constant}$  then :

$$\pi \frac{D_i^2}{4} = \pi \frac{D_{o1}^2}{4} + \pi \frac{D_{o2}^2}{4}$$

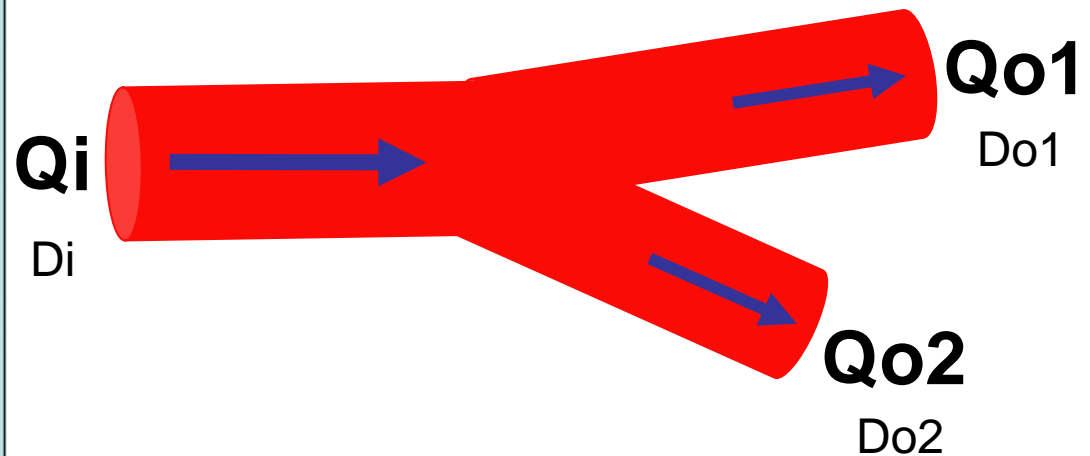
$$D_i = \sqrt{D_{o1}^2 + D_{o2}^2}$$

$$D_{o1} = D_{o2} = D_o$$

$$D_i = \sqrt{2D_o^2} = \sqrt{2}D_o$$

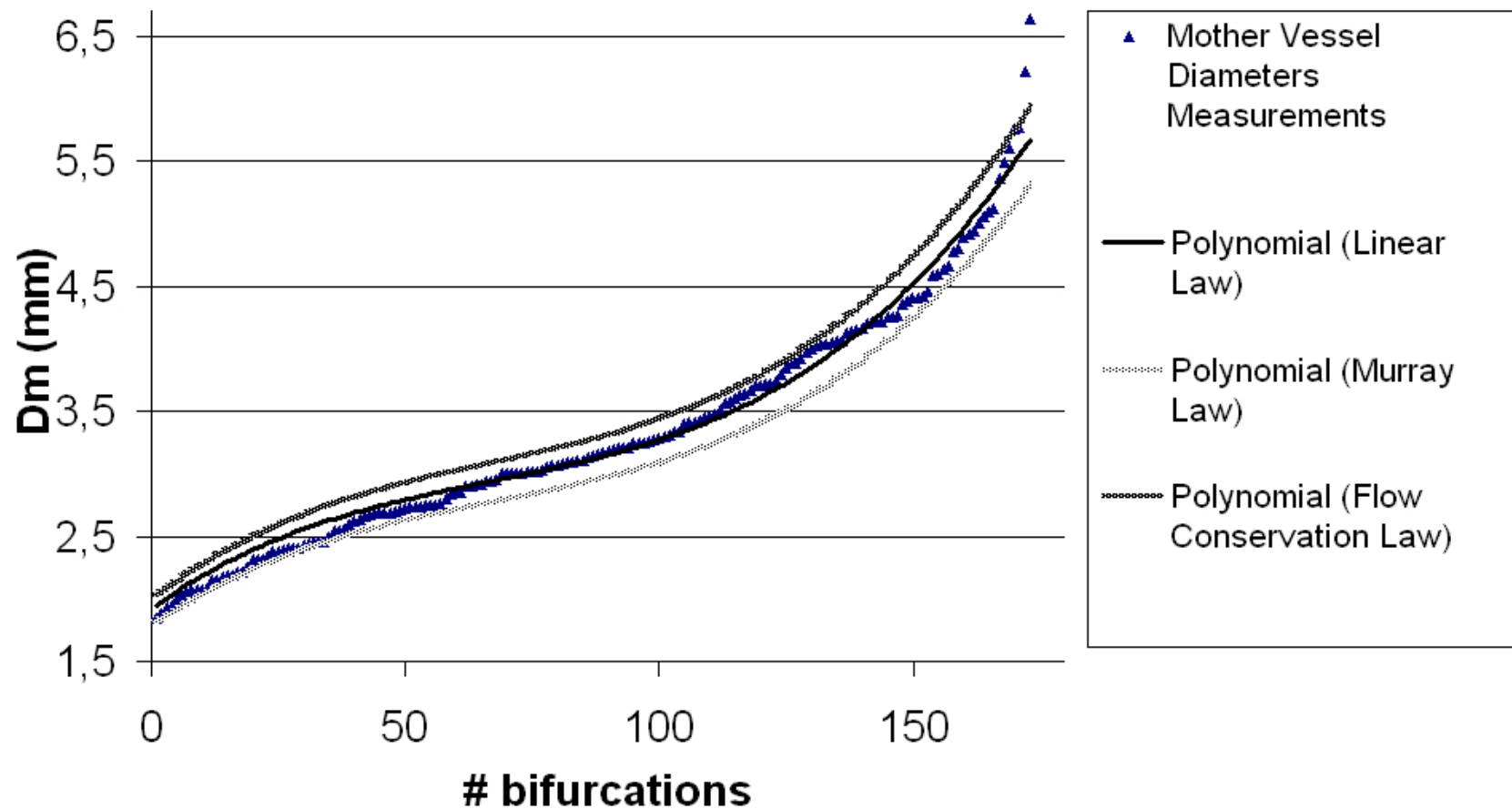
$$D_i = \sqrt{2}D_o = \frac{\sqrt{2}}{2}(D_{o1} + D_{o2})$$

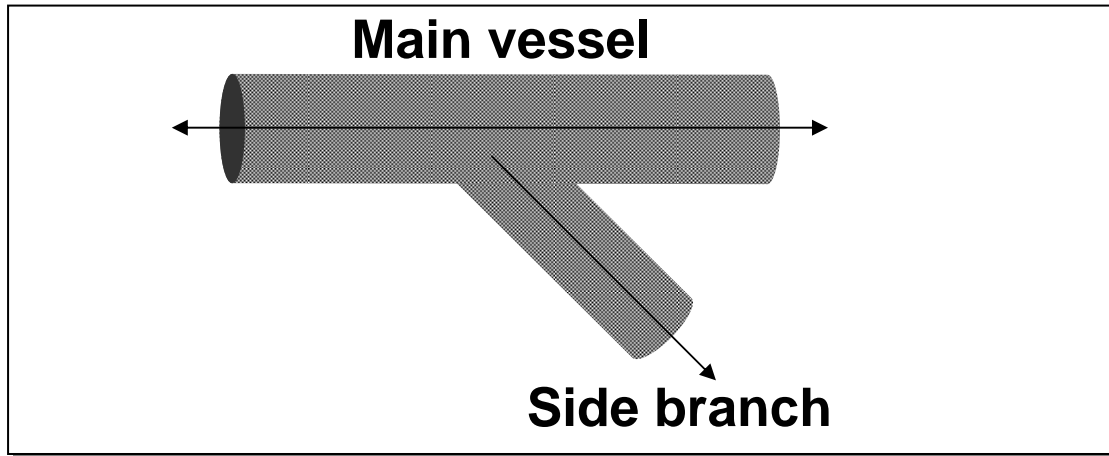
$$\frac{\sqrt{2}}{2} = 0.707 \quad \# \mathbf{0.678}$$



## Distribution of the 173 sets of mother-vessel diameters, as measured and calculated according to the 3 laws

*The linear law ( $R=0.678$ ) is found to be the most exact: the flow conservation law overestimates and Murray's law underestimates the calculated mother-vessel diameter*



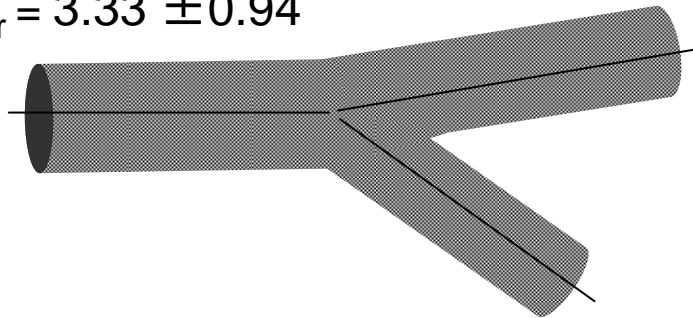


**Range [0.23 - 1.42 mm]**

$$\Delta D = 0.63 \pm 0.36 \text{ mm}$$

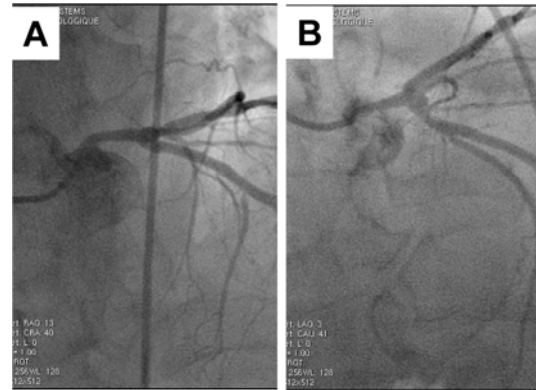
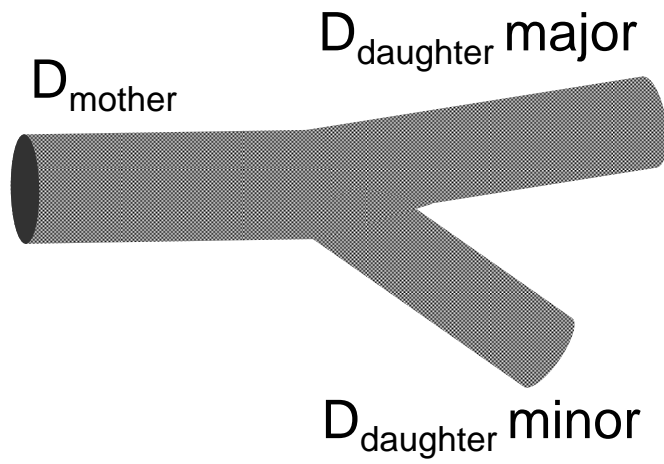
$$D_{\text{daughter major}} = 2.70 \pm 0.77 \text{ mm}$$

$$D_{\text{mother}} = 3.33 \pm 0.94 \text{ mm}$$



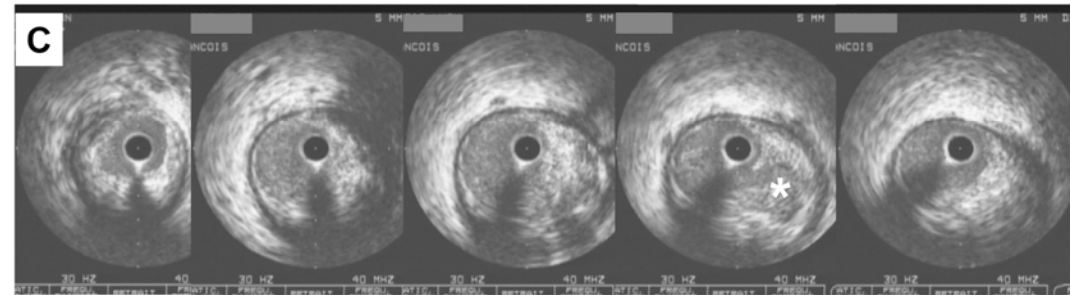
$$D_{\text{daughter minor}} = 2.23 \pm 0.68 \text{ mm}$$

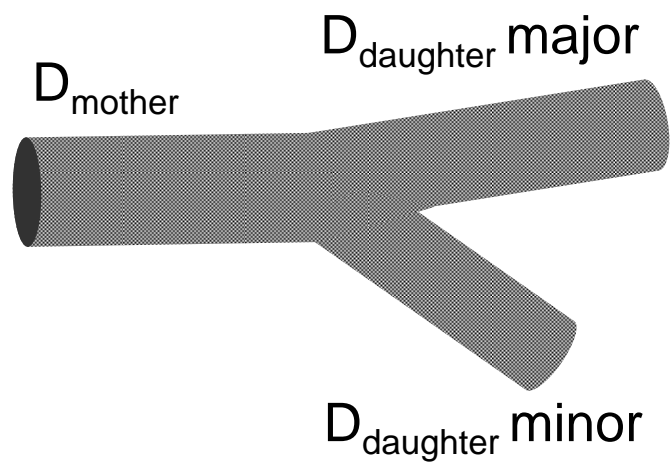
$$R_{\text{fractal}} = 0.678$$



$D_{\text{mother}}$  measured : 2.2 mm  
 $D_{\text{daughter 1}}$  measured : 3.1 mm  
 $D_{\text{daughter 2}}$  measured : 3.2 mm

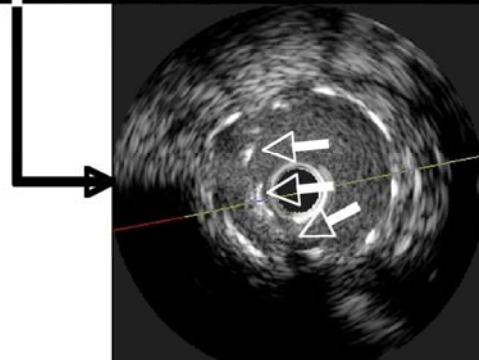
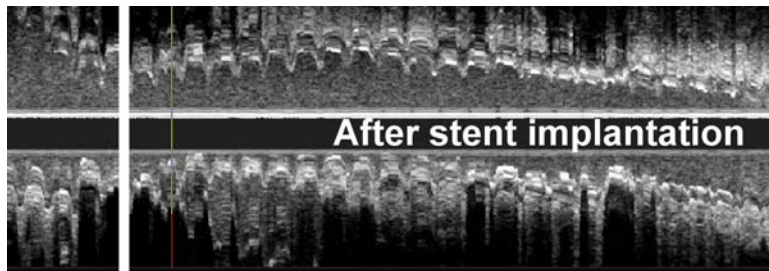
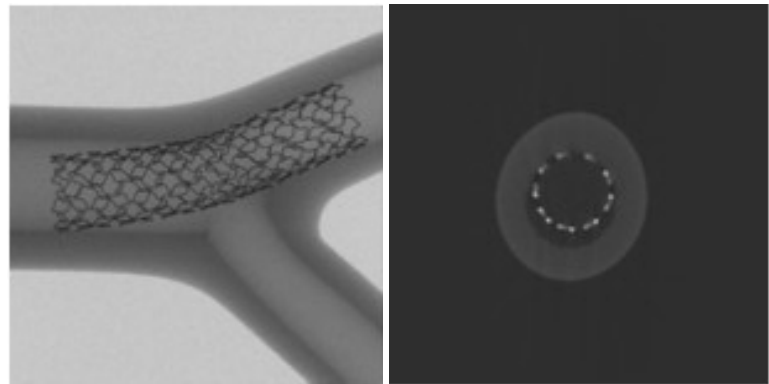
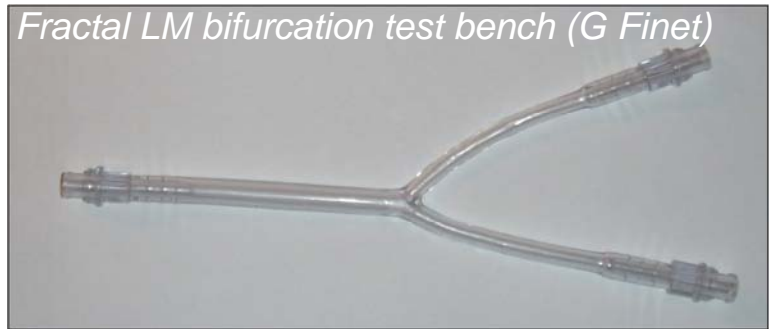
Expected  $D_{\text{mother}}$  (fractal ratio) : 4.22 mm  
Expected %D stenosis : 50%





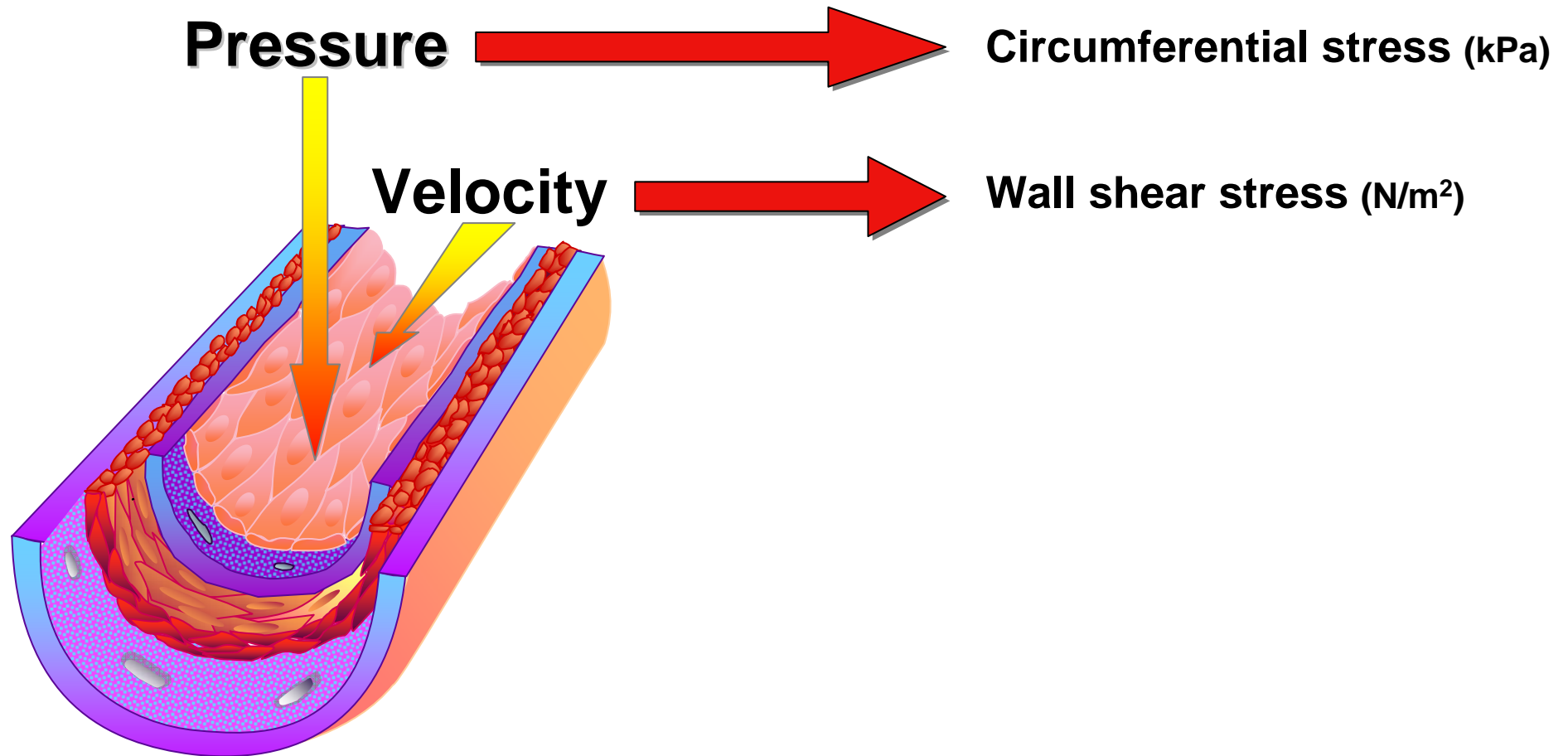
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Range [0.23 - 1.42 mm]

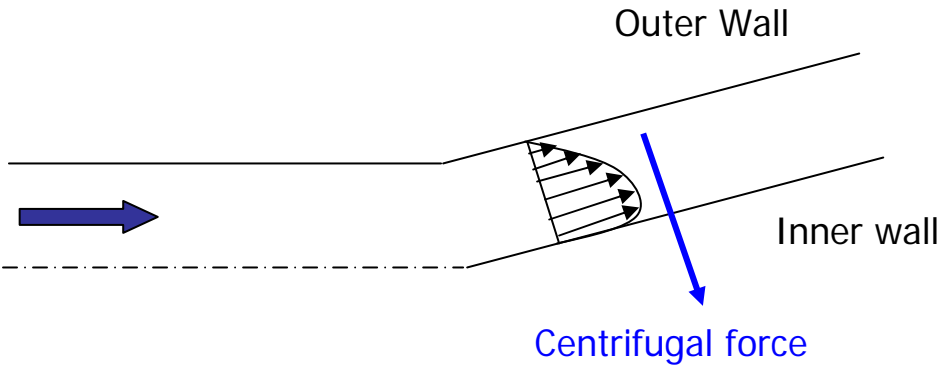
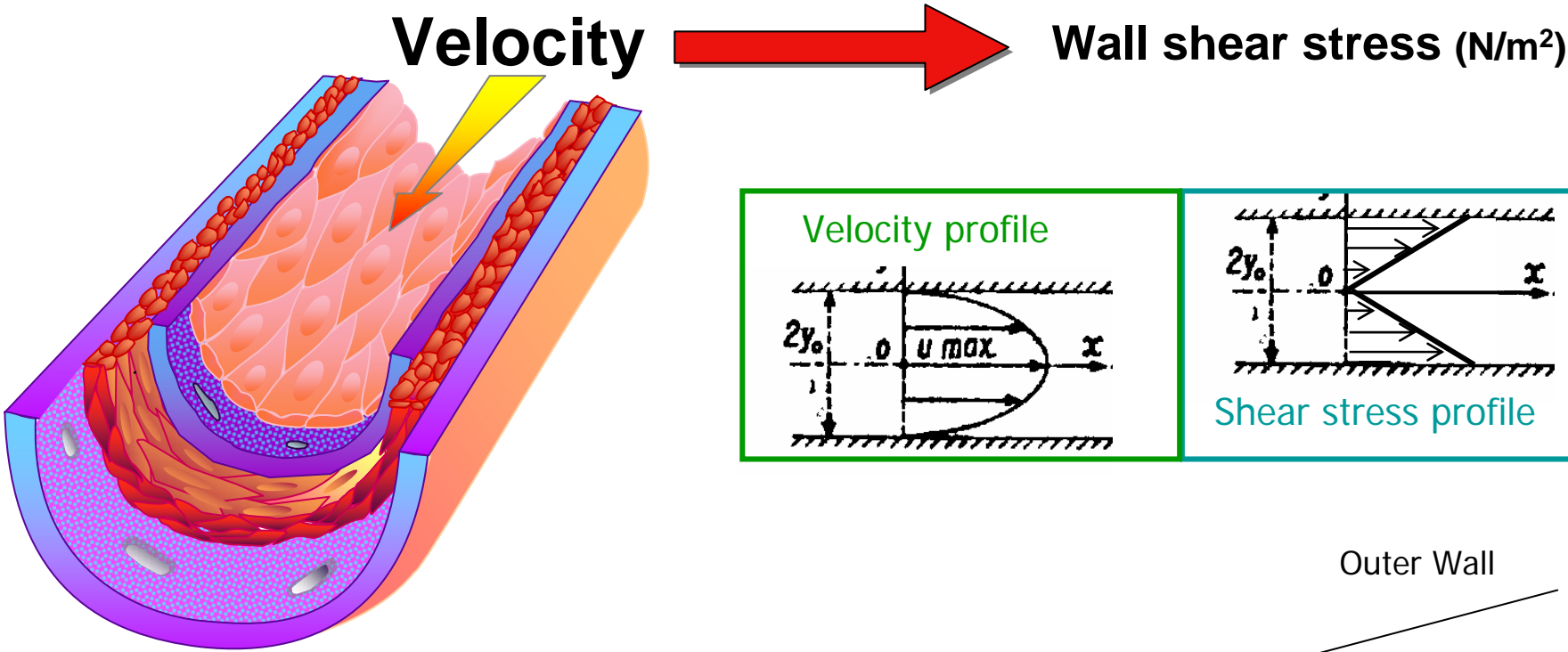




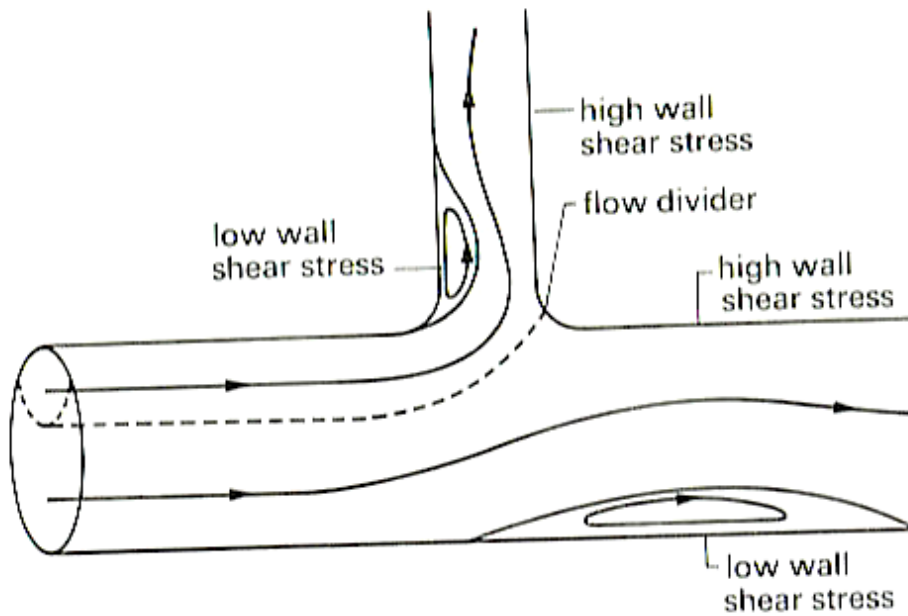
## Mechanical forces in the vascular wall



# Wall shear stress



# Wall shear stress distribution in bifurcation



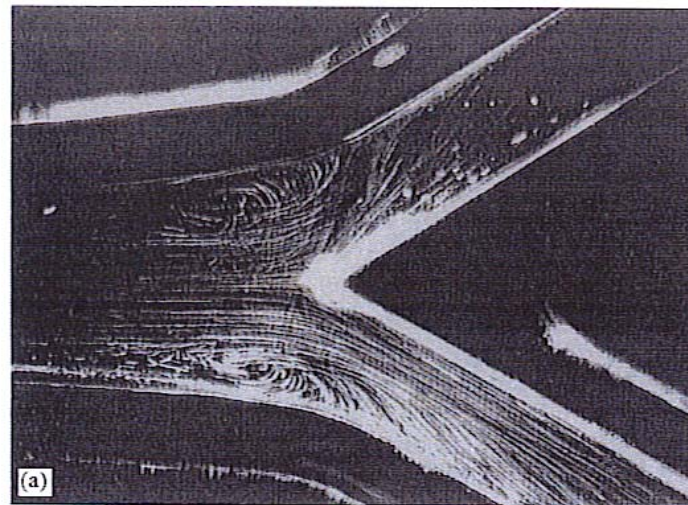
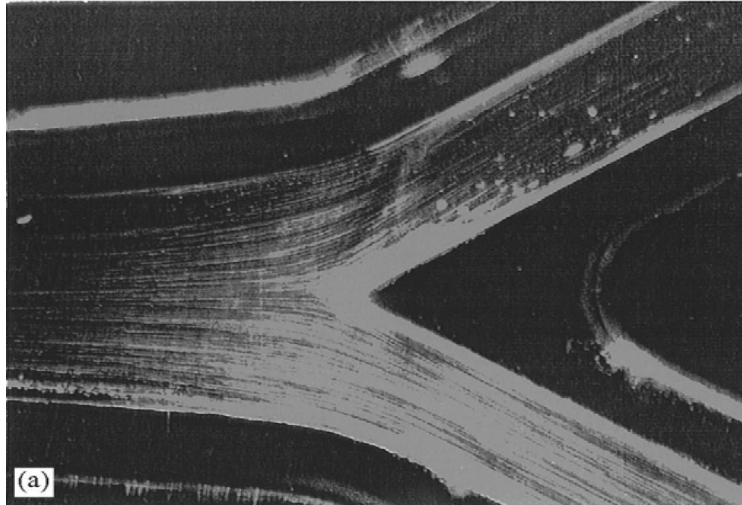
Taken from Caro et al, 1978



Taken from G. Giannakoulas (EBC 2008)

# Flow behaviour in an normal bifurcation

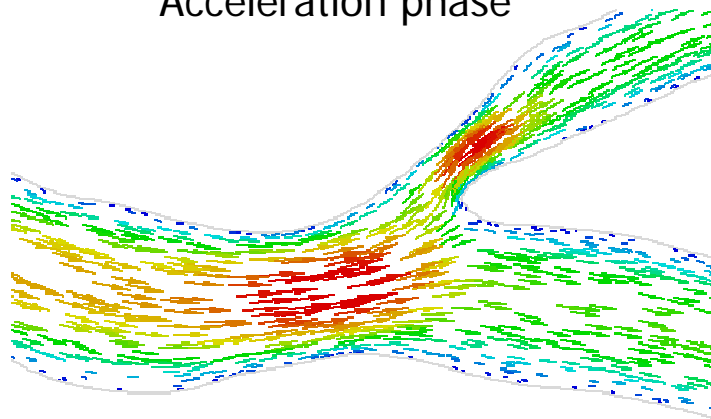
*Fabregues et al, 1998*



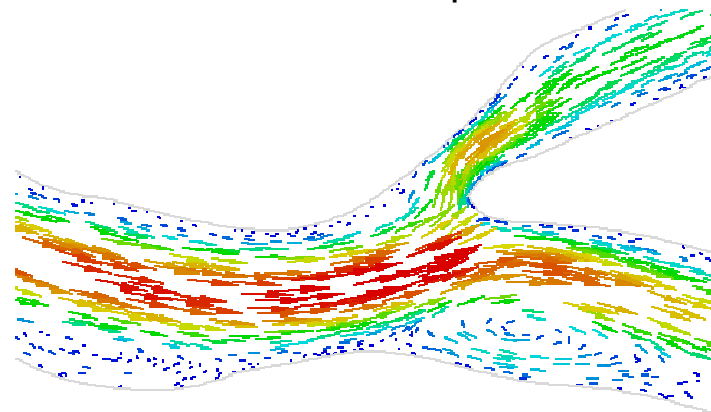
• High WSS at flow divider

• Low WSS at lateral walls

Acceleration phase



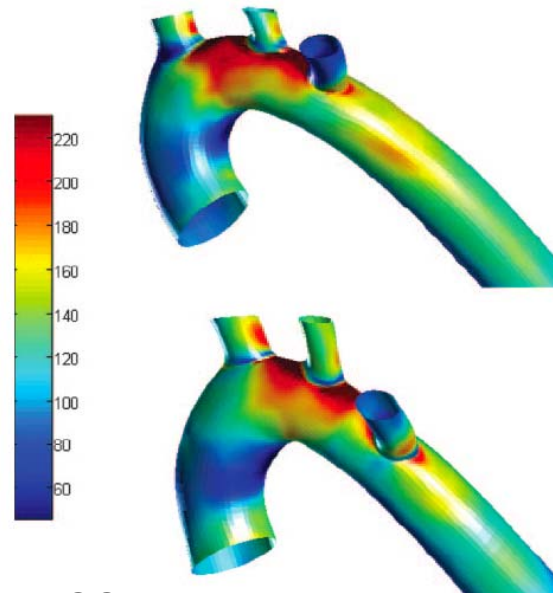
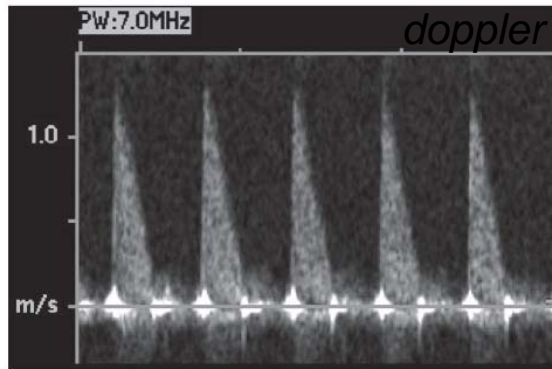
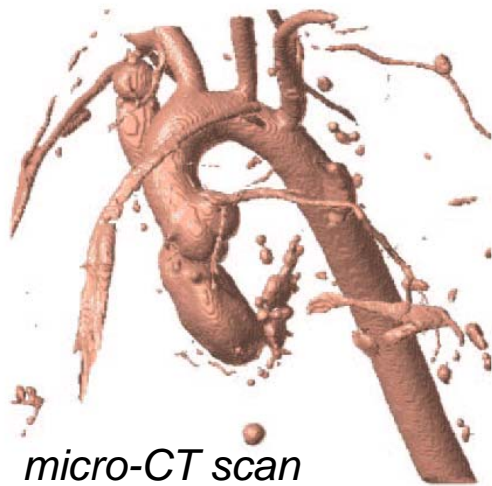
Deceleration phase



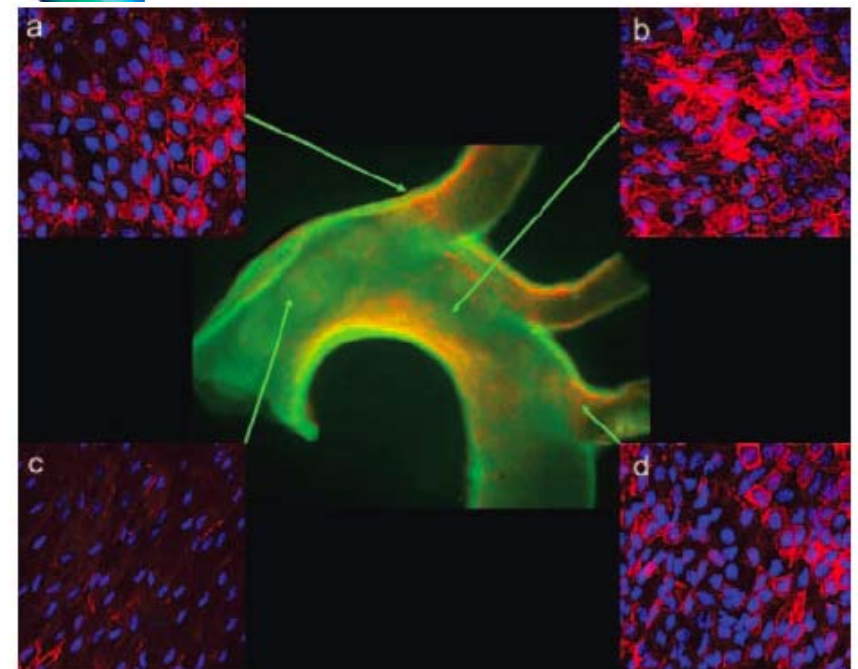
*G. Giannakoulas, G. Giannoglou, 2007*

# Hemodynamic Shear Stresses in Mouse Aortas

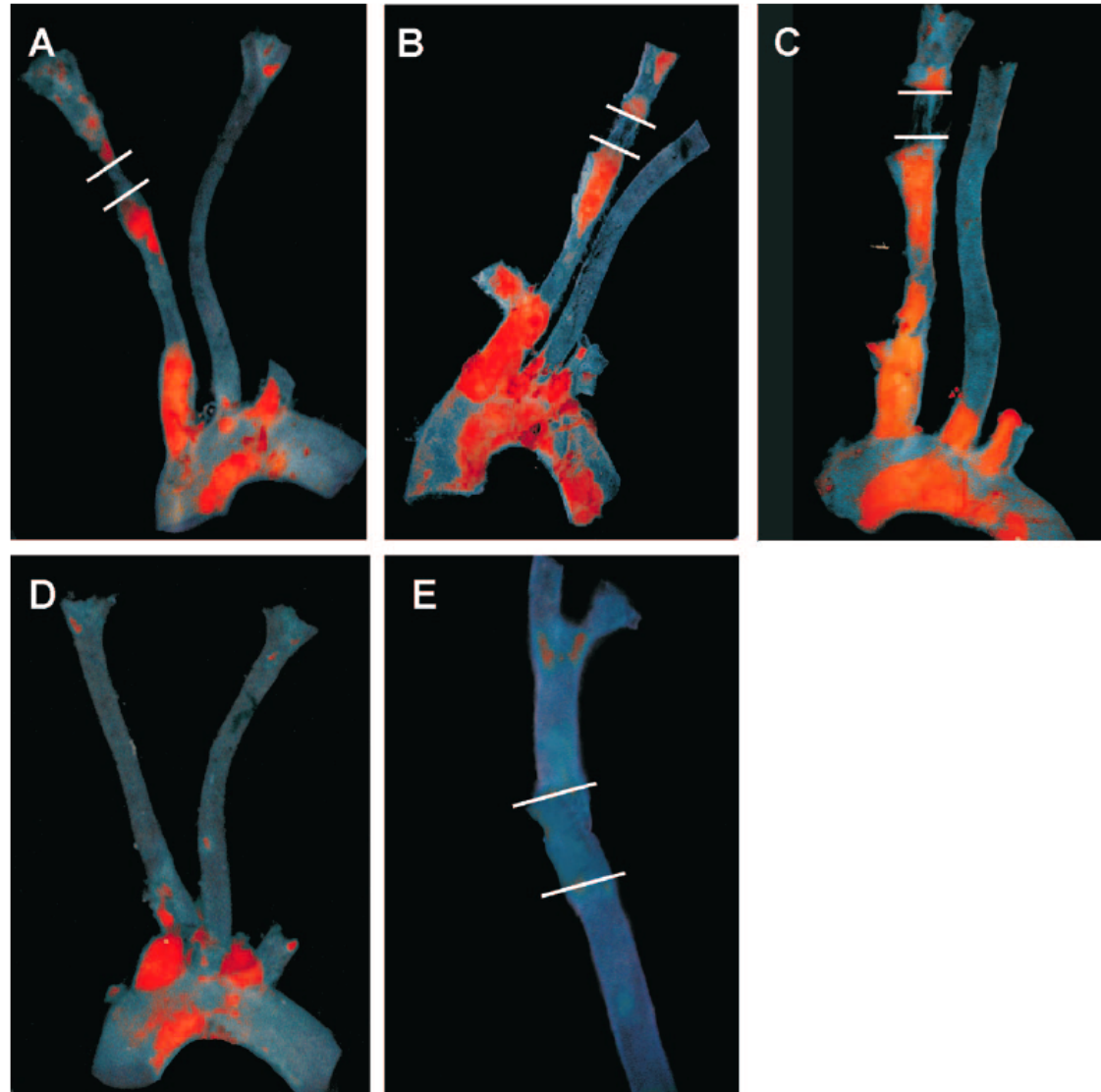
## *Implications for Atherogenesis*



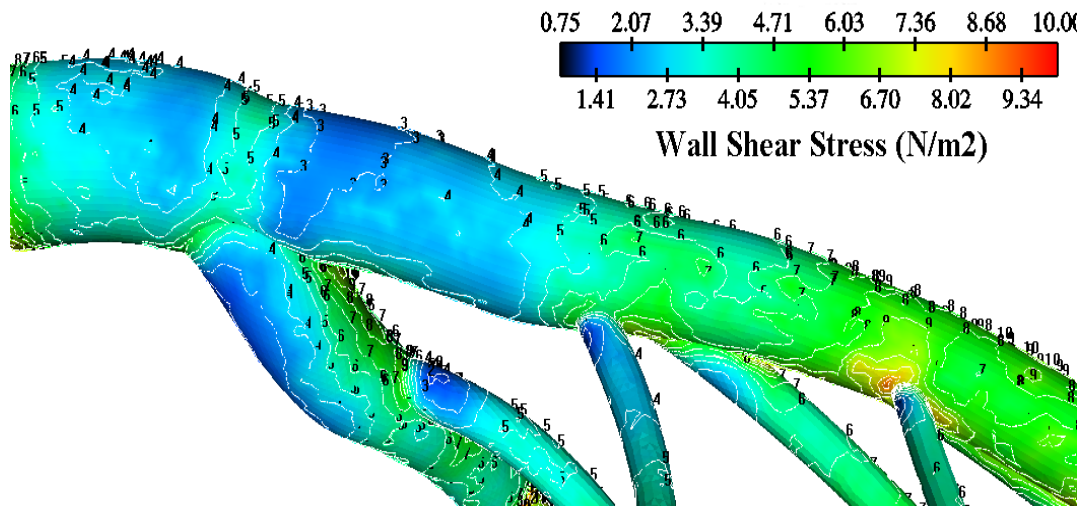
The differential localization of VCAM-1 protein expression



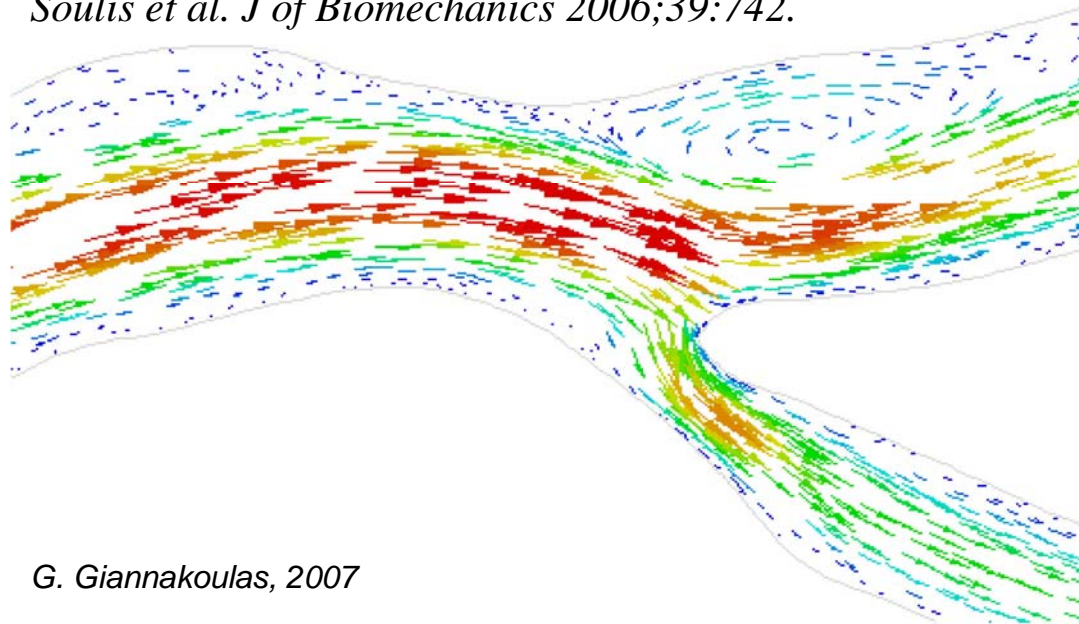
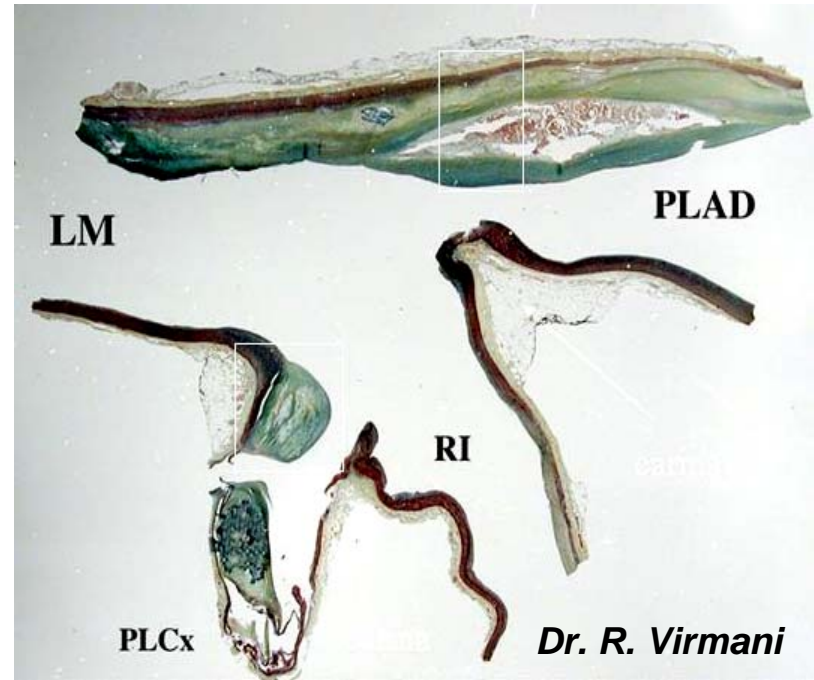
## Atherosclerotic lesion size and vulnerability are determined by patterns of fluid shear stress



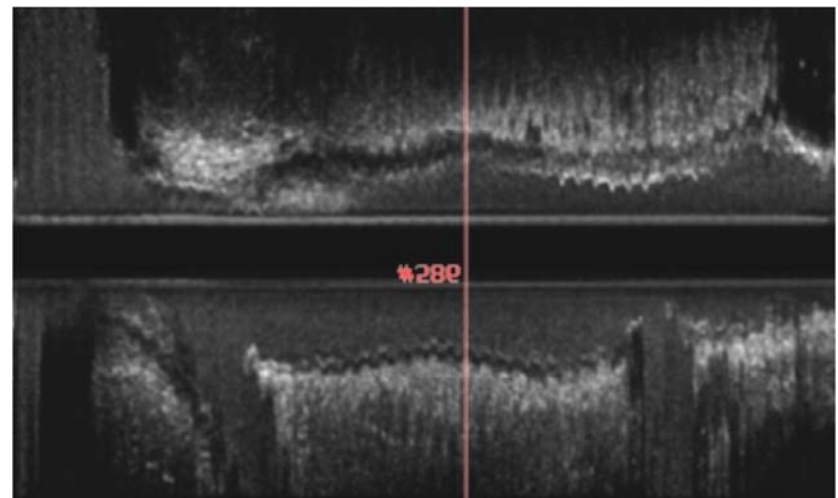
The distribution of the low WSS values  
is in accordance with the localization of atherosclerosis lesion  
(LM bifurcation)



Soulis et al. *J of Biomechanics* 2006;39:742.



G. Giannakoulas, 2007



## Plaque formation and Plaque progression

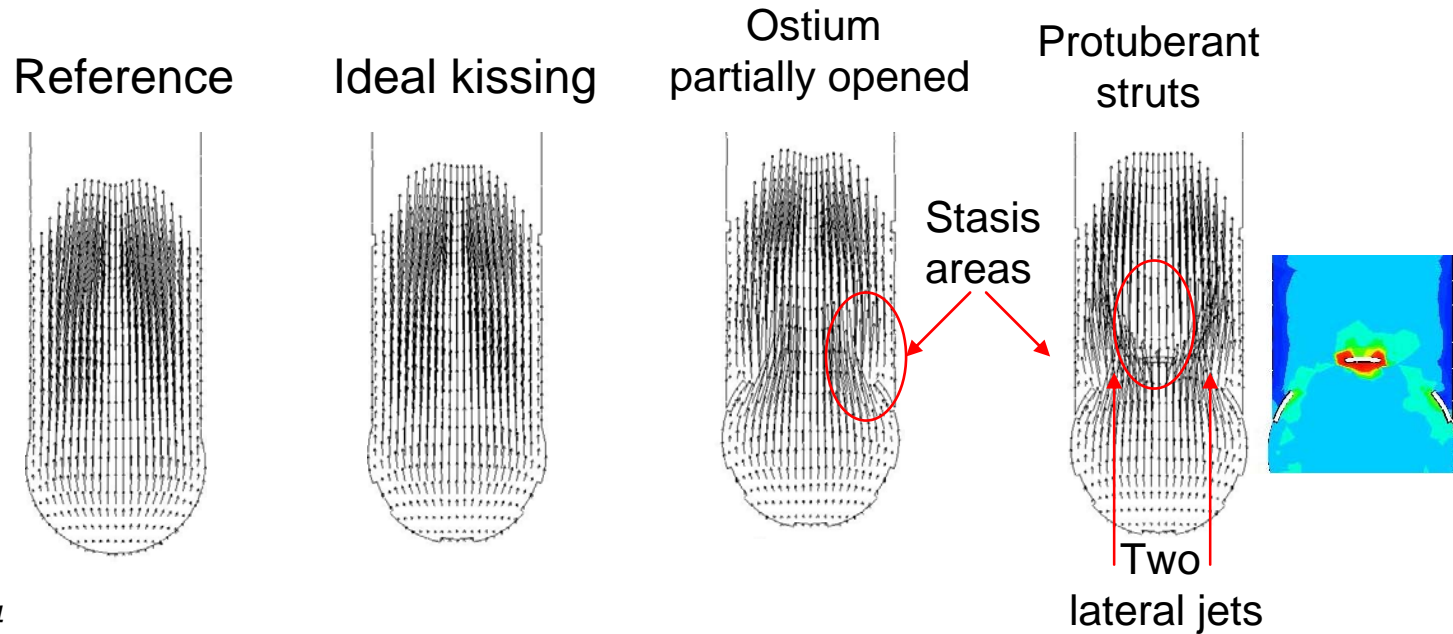
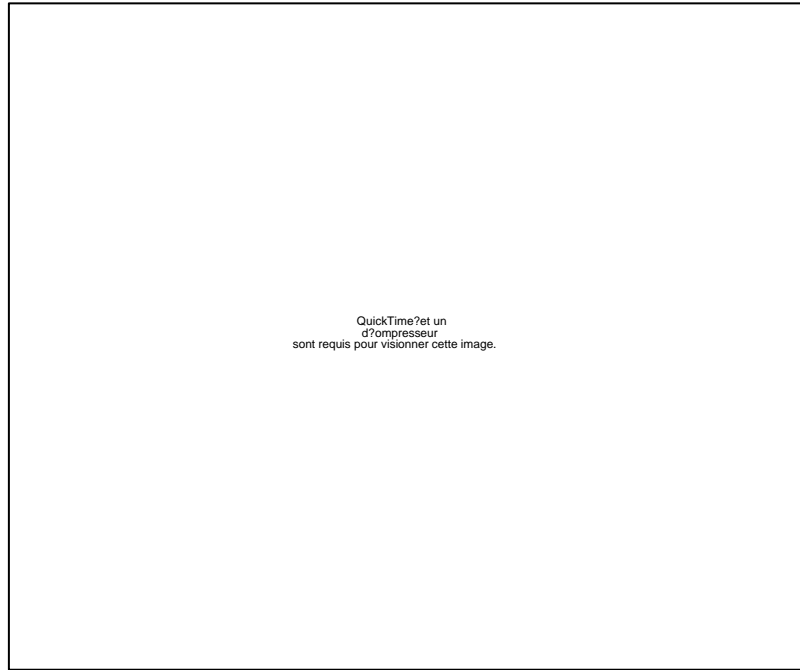
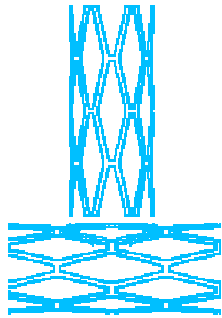


*adapted from G. Giannakoulas (EBC 2008)*



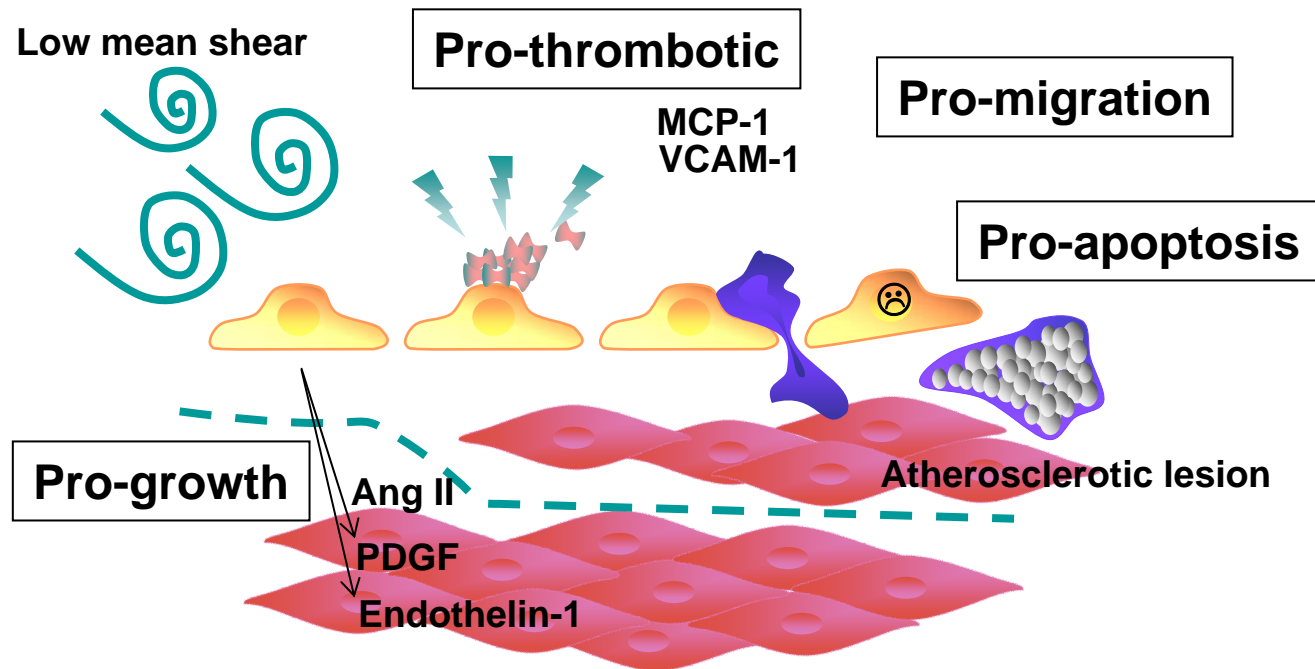
# Flow behaviour in a stented coronary bifurcation

Courtesy of Valérie Deplano



■ Recirculating zone and/or low Flow Favor Atherosclerosis or NIH

Traub & Berk, ATVB 1998  
Wentzel, 2001



■ Struts protruding into the lumen generate very high stent shear stress (swss) values  
Concomitant areas of high and low swss values favor:

- Platelet activation & deposition (Moake, 1988, Spijker, 2003)
- Thromboembolic complications (Bluestein, 2002)

Arterial bifurcation is *a morphological singularity of the vascular tree*

Despite its seeming complexity the vascular bifurcation tree turns out to be a sophisticated solution: *a maximum cost/benefit ratio*

Coronary bifurcation geometry is invariable whatever the observation scale and precisely described by a *fractal ratio*, this ratio can be very useful in our daily practice of angiography and angioplasty

$$D_{\text{mother vessel}} = \underline{0.678} (D_{\text{daughter vessel 1}} + D_{\text{daughter vessel 2}})$$

*Flow dynamics, rheology, and geometry interact*

*The occurrence of atherogenesis, atherosclerosis, and thrombosis are closely linked to local hemodynamic factors*

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***Stented bifurcation can become focus of flow disturbances and complications***